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## ABSTRACT

With sea ice in the Arctic continuing to shrink, the Arctic Ocean and the surrounding marginal seas will become more like the ocean at lower latitudes. In particular, with more open water, air-sea exchange will be more intense, and storms will be stronger and more frequent. The longer fetches over open water and the more energetic storms will combine to produce higher waves and more sea spray. Offshore structures—such as oil drilling, exploration, and production platforms—will face increased hazards from freezing sea spray.

Based on sea spray observations made with a cloud imaging probe at Mt. Desert Rock, an island off the coast of Maine, I quantify the spray that artificial islands built in the Arctic might experience. Mt. Desert Rock is small, low, unvegetated, and has an abrupt, rocky shoreline like these artificial islands. Many of the observations were at air temperatures below freezing. This paper reports the near-surface spray concentration and the rate of spray production at this rocky shoreline for spray droplets with radii from 6.25 to 143.75  $\mu\text{m}$  and for wind speeds from 5 to 17  $\text{m s}^{-1}$ . Spray concentration increases as the cube of the wind speed, but the shape of the concentration spectrum with respect to radius does not change with wind speed. Both near-surface spray concentration and the spray production rate are three orders of magnitude higher at this rocky shoreline than over the open ocean because of the high energy and resulting continuous white water in the surf zone.

## 1. Introduction

With the Arctic sea ice retreating farther and farther each summer, the Arctic Ocean is beginning to take on characteristics of the ocean at lower latitudes. In particular, heat lost from the now-open ocean can lead to more intense mesoscale storms; and the combination of storm winds and longer open water fetches will produce higher waves (e.g., Perrie et al. 2012; Asplin et al. 2012). Such evolving conditions will present new hazards for artificial structures like semi-submersible drilling rigs and man-made islands used as oil exploration and production platforms (Jones and Andreas 2009). Although the wind and waves themselves will create hazards for these structures, my interest here is the attendant sea spray produced.

Jones and Andreas (2009, 2012) previously considered the spray icing of semi-submersible drilling platforms that had fairly open profiles at the waterline such that most of the spray resulted from breaking waves in open water (also Minsk 1984a; Nauman 1984). Here, I turn to spray effects that small, artificial islands built in the Arctic Ocean can face: spray largely created by waves breaking along their shoreline. At sub-freezing temperatures, such spray will accumulate as ice on virtually all surfaces on these small islands (e.g., Minsk 1984b; Itagaki 1984). Even in above-freezing temperatures, the sea salt generated by high wind and waves will collect on raised structures and speed the corrosion of metal surfaces.

To quantify the rate of such shore-induced spray production, I carried out a month-long experiment in January 2013 on Mt. Desert Rock, an unvegetated island with low relief 24 miles out to sea from Bar Harbor, Maine. Mt. Desert Rock has a size and a topographic profile that is similar to some of the artificial islands now in the Arctic (e.g., Muzik and Kirby 1992; Gerwick 2007, Chapter 23). I presume that the spray concentrations and generation rates observed on Mt. Desert Rock will be similar to the values near other rocky shorelines and, in particular, will be

what artificial islands in the Arctic might experience in the coming decades.

Although the literature contains several papers that report sea spray observations at shorelines, my data are unique in several ways. Climatologically, Mt. Desert Rock in January provides a good chance of encountering sub-freezing air temperatures and winds high enough to produce copious spray. And, indeed, roughly half of my measurements were made at temperatures below freezing. I am unaware of other spray data collected at temperatures below freezing.

Secondly, most of the previous spray measurements from the coastal zone looked at only relatively small droplets. For example, de Leeuw et al. (2000), Vignati et al. (2001), Clarke et al. (2006), van Eijk et al. (2011), and Piazzola et al. (2015) all reported recent spray observations in coastal regions, and all sampled droplets with radii at formation as small as 0.02 to 0.1  $\mu\text{m}$ . Only van Eijk et al., however, sampled droplets with radii up to about 30  $\mu\text{m}$ ; the other papers reported on droplets with radii up to only 10–20  $\mu\text{m}$ . While these small droplets are plentiful, they do not carry enough mass to produce the severe icing that larger droplets do (Jones and Andreas 2012).

Therefore, on Mt. Desert Rock, I collected spray data with a cloud imaging probe for which the smallest radius bin was centered at 6.25  $\mu\text{m}$  and the instrument was capable of counting droplets with radii up to 775  $\mu\text{m}$ . Although the counting statistics were poor for the largest droplets, I do report here spray concentration measurements for droplets in a radius bin centered at 143.75  $\mu\text{m}$ —well into what is referred to as the *spume* regime for open ocean spray. Thus, I believe these observations represent the largest spray droplets that have been measured near a shoreline.

In this paper, I report data from the cloud imaging probe deployed for 27 days near the

107 shoreline on Mt. Desert Rock. These data span 12.5- $\mu\text{m}$ -wide radius bins with centers ranging  
108 from 6.25 to 143.75  $\mu\text{m}$  and include 10-m winds from 5 to 17  $\text{m s}^{-1}$ . A key finding is that the  
109 droplet spectra have the same shape at all observed wind speeds. I am thus able to derive an  
110 expression for the near-surface droplet concentration as the product of a function of just droplet  
111 radius and another function that goes as the cube of the wind speed. This concentration function,  
112 lastly, yields a function for predicting spray generation when ocean waves encroach on a rocky  
113 (as opposed to a sloping, sandy) shoreline.  
114

## 2. Measurements on Mt. Desert Rock

Mt. Desert Rock, 24 miles into the Atlantic east of Bar Harbor, Maine, has a lightkeeper's house and a stone lighthouse that NOAA has instrumented as a C-MAN station under the National Data Buoy Center (NDBC). The College of the Atlantic in Bar Harbor owns Mt. Desert Rock and, as such, facilitates access to the "Rock" and provided us logistics support.

Figure 1 shows how small Mt. Desert Rock is and identifies the permanent structures there and the 2013 instrument locations. The "Rock" is truly a desert island: Its surface has no vegetation but is simply a rocky outcrop. From our survey (these numbers may differ from the NDBC information), the high point of the island is only 9.2 m above mean sea level; the lighthouse is 18 m tall. Prevailing winds at Mt. Desert Rock in January are westerly and northwesterly. We placed all instruments for best exposure to these winds.

To provide a rigid base and some security for the expensive cloud imaging probe (CIP; from Droplet Measurement Technologies), we mounted it on the foghorn platform (Fig. 1). As such, the probe was 3.24 m above local ground and 8.66 m above mean sea level. Because the wind speed and direction through the probe's laser array are crucial for computing spray concentration, the cloud imaging probe was rigidly attached to a Gill WindMaster sonic anemometer/thermometer (Fig. 2). The sonic's sample area was 0.48 m above the CIP's laser array. We frequently rotated this whole system to orient the cloud imaging probe into the wind. The appendix summarizes the equations that I used for obtaining spray concentration from the CIP.

To document near-surface meteorological conditions during our measurements, we deployed a "turbulence tripod" near the high-water line (Fig. 1). This tripod held a three-axis sonic anemometer/thermometer from Applied Technologies, Inc. (ATI), 2.35 m above ground, a

Li-Cor water vapor and carbon dioxide sensor 2.10 m above ground, and an Ophir hygrometer (which also measured air temperature) 2.23 m above ground. The ground here was 4.4 m above mean sea level.

I supplemented our own measurements with the NOAA measurements from the Mt. Desert Rock lighthouse; from another NOAA C-MAN station on nearby Matinicus Rock; and from two nearby buoys, 44034 and 44037, owned and maintained by the Northeastern Regional Association of Coastal Ocean Observing Systems.

Figures 3 and 4 show time series of meteorological and oceanographic data for January 2013 from these various sources. The winds denoted “MDR NOAA” and “Matinicus” were measured by the C-MAN instruments high on the Mt. Desert Rock and Matinicus lighthouses, respectively, and thus show higher speeds than the measurements nearer the surface from the two buoys and from the ATI and Gill sonics. These latter data are more representative of the wave and spray conditions and show that we sampled in winds up to about  $17 \text{ m s}^{-1}$ . The temperature panel in Fig. 3 shows that air temperatures were always less than  $10^{\circ}\text{C}$  during the measurements and were frequently below freezing. The stratification was generally unstable (water warmer than air; Figs. 3 and 4).



### 3. Data analysis

The appendix reviews the equations I used for processing measurements from the cloud imaging probe. Briefly, I computed spray concentrations in 12 radius bins, each 12.5- $\mu\text{m}$  wide, from zero to 150  $\mu\text{m}$ . The center radius in each bin locates the bin average in the upcoming plots and calculations.

The cloud imaging probe ran continuously, except when we stopped recording to reorient it into the wind. As such, from its 1 Hz measurements, I computed half-hour averages of spray concentrations for the first 30 minutes of an hour and for the second 30 minutes. For instances when the recording did not start at the top of the hour or end exactly at the top of the hour, I still computed averages from these partial 30-minute runs. I did, however, later exclude runs that were shorter than 15 minutes.

For the CIP site on Mt. Desert Rock, the counting statistics for the largest bins that the cloud imaging probe could sample were poor. Hence, the bin centered at a radius of 143.75  $\mu\text{m}$  was the largest one that I retained for analysis. Moreover, for any bin, I retained its average only if it had counted at least ten droplets during the averaging period.

The Gill sonic anemometer attached to the cloud imaging probe sampled the three wind components and the sonic temperature roughly six times per second. I averaged these data over the same averaging periods as for the CIP. From the average along-wind ( $\bar{U}$ ) and cross-wind ( $\bar{V}$ ) components, I could compute the wind's average attack angle into the laser array of the cloud imaging probe. If this attack angle is not small, droplets hitting the thin arms that extend from the body of the CIP and hold the laser array (Fig. 2) can shatter; and the resulting smaller droplets can pass through the array and be counted. To minimize these erroneous counts, I kept for analysis only runs for which the attack angle of the wind was between  $-20^\circ$  and  $+20^\circ$ .

From  $\overline{U}$ ,  $\overline{V}$ , and a measurement of the CIP's angular orientation, I also calculated the wind direction at the CIP in a true-north coordinate system. Figure 1 shows that for wind directions between  $260^\circ$  and  $7^\circ$  the CIP had best exposure to the ocean. My analysis includes only runs for which the average wind direction at the CIP was in this sector.

I also sequenced the analysis with the nearest tidal record, from Bar Harbor (NDBC station 8413220), and thereby assigned each half-hour run a tidal height. The arcs at 50 and 75 m in Fig. 1 show that, at high tide, the cloud imaging probe was well within 50 m of open water. Even at low tide, it was no more than about 75 m from open water and was often much closer.

Nevertheless, to judge whether distance from the water affected the spray counts, subsequent plots distinguish between the data collected during high water and low water. The tidal range during our observations was  $-0.43$  to  $3.93$  m. Therefore, I designate as *low water* runs those collected when the tide was between  $-0.43$  and  $1.75$  m; *high water* runs were collected when the tide was between  $1.75$  m and  $3.93$  m.

For measurements over the ocean, the neutral-stability wind speed at 10 m,  $U_{N10}$ , is commonly the independent variable in analyses and plots. I obtained  $U_{N10}$  from the Gill sonic. Its measurements of the three wind components yielded  $U_z$ , the average wind speed at height  $z_s$  for each half-hour CIP run. Similarity theory (e.g., Panofsky and Dutton 1984, p. 134) then relates  $U_z$  to the wind speed at 10 m:

$$U_{10} = U_z + \frac{u_*}{k} \left[ \ln \left( \frac{10}{z_s} \right) - \psi_m \left( \frac{10}{L} \right) + \psi_m \left( \frac{z_s}{L} \right) \right]. \quad (3.1)$$

Here,  $u_*$  is the friction velocity;  $k$  ( $= 0.40$ ) is the von Kármán constant;  $z_s$  ( $= 3.72$  m) is the height of the Gill sonic above the local surface; and  $\psi_m$  is a stratification correction that is a function of

200 the Obukhov length,  $L$ .

201 Because, in subsequent analyses I ignore runs for which the 10-m wind speed was less  
202 than  $5 \text{ m s}^{-1}$  (because there was negligible spray) and because  $z_s$  and 10 m are relatively small, I  
203 ignore the stratification corrections in (3.1) because they are small. Hence, (3.1) yields a simpler  
204 expression for  $U_{N10}$ :

$$205 \quad U_{N10} = U_z + \frac{u_*}{k} \ln \left( \frac{10}{z_s} \right). \quad (3.2)$$

206 Meanwhile, Andreas et al. (2012) deduced a relationship between  $u_*$  and  $U_{N10}$  from  
207 several thousand observations over the open ocean:

$$208 \quad u_* = 0.239 + 0.0433 \left\{ (U_{N10} - 8.271) + \left[ 0.120 (U_{N10} - 8.271)^2 + 0.181 \right]^{1/2} \right\}. \quad (3.3)$$

209 Here, both  $u_*$  and  $U_{N10}$  are in  $\text{m s}^{-1}$ . Substituting (3.3) for  $u_*$  in (3.2) yields a single equation that  
210 relates the measurement,  $U_z$ , to the desired quantity,  $U_{N10}$ . I solved it using Newton's method  
211 and thereby obtained values for both  $U_{N10}$  and  $u_*$  for each CIP run.

212 To standardize the spray concentrations to a common height that will also be relevant for  
213 estimating the spray generation function, I extrapolated the spray observations to the height of  
214 the wave crests. I designate these concentrations  $C_0$  and interpret them as the concentration at  
215 the sea surface (e.g., Fairall et al. 2009; Andreas et al. 2010). Fairall et al. (2009) used the  
216 following relation to convert the spray concentration at height  $z_1$  to the concentration at height  $z_2$ :

$$217 \quad C(z_2, r_0) = C(z_1, r_0) \left( \frac{z_2}{z_1} \right)^{-V_g(r_0)/k u_* f_s}. \quad (3.4)$$

218 Here, both concentrations are for droplets with a radius at formation of  $r_0$ ,  $V_g(r_0)$  is the terminal  
219 fall speed of these droplets, and  $f_s$  is related to the turbulent diffusivity of the droplets.

220 Because I want to estimate  $C_0$ ,  $z_2$  becomes  $H_{1/3}/2$  ( $= A_{1/3}$ ), the significant wave amplitude,

where  $H_{1/3}$  is the significant wave height (Fig. 4). In other words,  $z_2$  is the average height above mean sea level of the wave crests. Fairall et al. (2009), among others, assume that  $C(z_2, r_0)$  is constant between  $A_{1/3}$  and the mean water surface. Consequently,  $C(A_{1/3}, r_0)$  is a reasonable estimate for  $C_0$ . As such, (3.4) becomes

$$C_0(r_0) = C(z_{CIP}, r_0) \left( \frac{A_{1/3}}{z_{CIP}} \right)^{-V_g(r_0)/k u_* f_s}, \quad (3.5)$$

where  $z_{CIP}$  is the height of the cloud imaging probe above the local surface.

For  $f_s$  in (3.5), I use (Rouault et al. 1991; Kepert et al. 1999; Fairall et al. 2009)

$$f_s(r_0, u_*) = \frac{1}{1 + 2[V_g(r_0)/\sigma_w]^2}, \quad (3.6)$$

where  $\sigma_w$  is the standard deviation of the vertical velocity fluctuations of the air. Continuing with the assumption of near-neutral-stratification, I use for  $\sigma_w$  in (3.6)  $1.25 u_*$  (Kaimal and Finnigan 1994, p. 16).

Lastly,  $A_{1/3}$  in (3.5) comes from the algorithm that Andreas and Wang (2007) derived from data collected by NDBC buoys off the northeast coast of the United States, including several in the vicinity of Mt. Desert Rock. Figure 4 compares the estimates of  $H_{1/3}$  from this algorithm with the data from buoys 44034 and 44037. Agreement between the Andreas and Wang algorithm and the buoy data is generally good, but the Andreas and Wang algorithm does predict a non-zero lower limit for  $H_{1/3}$  in light winds. This lower limit is obvious in Fig. 4 but is not an issue for this analysis because it occurs when the wind speed was less than  $5 \text{ m s}^{-1}$ , and I ignore these wind speeds in the upcoming results.

#### 4. Sea spray concentration

Figures 5 and 6 show the near-surface spray droplet concentration spectra (i.e.,  $C_0$ ) as measured by the cloud imaging probe. Each panel breaks out measurements for wind speeds ( $U_{N10}$  in this case) in ranges between 6 and 17 m s<sup>-1</sup>. Each panel also identifies measurements made during high water and low water.

Figures 5 and 6 do not reveal any obvious differences between the measurements made during high water and low water. Both the magnitude of the concentrations and the shape of the spectra as a function of radius are similar for the two types of observations.

In fact, in Figs. 5 and 6, the spectral shape seems to be the same for all wind speeds. I therefore nondimensionalized all the spectra in Figs. 5 and 6 with the concentration measured at  $r_0 = 6.25 \mu\text{m}$  for each spectrum. Figure 7 plots nondimensional versions of all 363 spectra collected in wind speeds of 5 m s<sup>-1</sup> and higher. Still here, the figure distinguishes the 170 spectra collected during high water from the 163 spectra collected during low water to reiterate that the distance to open water does not seem to have influenced the results. That is, the medians for all the data in a radius bin and the medians for just the high water and low water observations in a bin are all largely indistinguishable.

The four small-radius bins in Fig. 7 fall on a straight line on this log-log plot,

$$\ln[C_0(r_0)/C_0(r_0=6.25\mu\text{m})] = 3.39396 - 1.85201\ln(r_0); \quad (4.1)$$

the six large-radius bins similarly fall along another straight line,

$$\ln[C_0(r_0)/C_0(r_0=6.25\mu\text{m})] = 21.71391 - 6.31974\ln(r_0). \quad (4.2)$$

I can therefore derive a hyperbola to fit the entire nondimensional spectrum,

$$\ln[C_0(r_0)/C_0(r_0=6.25\mu\text{m})] = -4.20022 - 4.08587 \left\{ [\ln(r_0) - 4.10051] + \left\{ 0.29891[\ln(r_0) - 4.10051]^2 + 0.78383a^2 \right\}^{1/2} \right\}. \quad (4.3)$$

Here,  $a$  is a coefficient that moves the knee of the hyperbola as close to the intersection of lines (4.1) and (4.2) as I desire;  $a = 0.10$  produces the best-fitting hyperbola. Figure 7 shows this result.

Conceptually, we can use (4.3) to predict spray concentration if we can associate a wind speed dependence for the spectra plotted in Figs. 5 and 6. All we need to know is how  $C_0(r_0 = 6.25 \mu\text{m})$ , the concentration for droplets in the bin centered at  $6.25 \mu\text{m}$  used to nondimensionalized the spectra in Fig. 7, depends on wind speed.

To evaluate this wind speed dependence, I first looked at the wind speed dependence of all the concentration data because any wind speed dependence that I assign to the  $6.25\text{-}\mu\text{m}$  radius bin must be appropriate for all radius bins up to  $143.75 \mu\text{m}$ . Figure 8 therefore plots normalized droplet concentrations from all 333 droplet spectra. I calculated these normalized concentrations by dividing all concentrations in a specific radius bin by the average concentration for that bin. Consequently, the normalized concentrations in Fig. 8 tend to distribute equally below and above one.

I fitted straight lines through the log-log data in Fig. 8. The standard approach is to do least-squares linear regression with  $y$  as the dependent variable and  $x$  as the independent variable. When both  $x$  and  $y$  have comparable uncertainties, however, such a fitting can be biased because least-squares algorithms presume that the  $x$  values are perfectly known. Consequently, I also like to derive a fitting relation from the bisector of  $y$ -versus- $x$  and  $x$ -versus- $y$  least-squares fits (e.g., Andreas 2002a). Figure 8 also shows this bisector fit. Lastly, since both fitting lines are close to cubic in wind speed, Fig. 8 shows the cubic relation for which the normalized concentration goes

284 as  $U_{N10}^3$ .

285 In Fig. 8, the cubic relation splits the  $y$ -versus- $x$  and bisector fits and, by eye, does best at  
286 representing the data for all radius bins and for all wind speeds. I thus represent the  
287 concentration data for the 6.25- $\mu\text{m}$  radius bin with a cubic relation in  $U_{N10}$ . Figure 9 shows that  
288 representation, which is

$$289 \quad C_0(r_0=6.25\mu\text{m}) = 100.38U_{N10}^3. \quad (4.4)$$

290 This gives  $C_0(r_0 = 6.25 \mu\text{m})$  in  $\text{m}^{-3} \mu\text{m}^{-1}$  for  $U_{N10}$  in  $\text{m s}^{-1}$ .

291 I close the discussion of Fig. 8 by pointing out, again, that the data collected during high  
292 water do not differ appreciably from the data collected during low water.

293 Combining (4.4) and (4.3) produces an expression to fit the near-surface spray  
294 concentrations measured on Mt. Desert Rock:

$$295 \quad C_0(r_0, U_{N10}) = 100.38U_{N10}^3 \exp[-4.20022 \\ -4.08587 \left\{ \left[ \ln(r_0) - 4.10051 \right] + \left\{ 0.29891 \left[ \ln(r_0) - 4.10051 \right]^2 + 0.0078383 \right\}^{1/2} \right\}]. \quad (4.5)$$

296 Again,  $C_0$  is in  $\text{m}^{-3} \mu\text{m}^{-1}$  when  $U_{N10}$  is in  $\text{m s}^{-1}$  and  $r_0$  is in  $\mu\text{m}$ .

297 With the green curves, each panel in Figs. 5 and 6 displays (4.5), where  $U_{N10}$  for each  
298 green curve is taken as the mid-range wind speed for the wind speed range indicated in the panel.  
299 I draw two conclusions from these green curves. First, the shape of the droplet spectra is  
300 consistent for all the wind speeds depicted. Second, the cubic dependence on  $U_{N10}$  does well in  
301 representing the spectral levels at all wind speeds in the dataset.

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## 5. Spray generation function

The spray generation function, which I henceforth denote as  $dF/dr_0$  (e.g., Monahan et al. 1986; Andreas 2002b), predicts the number of spray droplets with initial radius  $r_0$  that are produced per square meter of sea surface per second per micrometer increment in droplet radius. Its units are thus  $\text{m}^{-2} \text{s}^{-1} \mu\text{m}^{-1}$ , where  $r_0$  is expressed in micrometers.

Often,  $dF/dr_0$  is calculated as the near-surface droplet concentration,  $C_0(r_0)$ , times some velocity scale (e.g., Moore and Mason 1954; Fairall and Larsen 1984; Smith et al. 1993; Lewis and Schwarz 2004, p. 101; Hoppel et al. 2005; de Leeuw et al. 2011). This approach makes the reasonable assumption that, to be observed, spray droplets need some upward velocity to be entrained in the air flow. Andreas et al. (2010) evaluated the usefulness of this approach for four distinct velocity scales—the dry deposition velocity, which can be close to the terminal fall velocity; a turbulent droplet diffusion velocity; the jet droplet ejection velocity; and the wind speed evaluated at the significant wave amplitude,  $U_{A/3}$ . For the droplets like those observed at Mt. Desert Rock—with radii of about  $10 \mu\text{m}$  and larger—Andreas et al. concluded that  $U_{A/3}$  is the best velocity scale for predicting spray generation from the near-surface concentration. Therefore, I estimate the spray generation function as

$$\frac{dF}{dr_0} = U_{A/3} C_0(r_0, U_{N10}), \quad (5.1)$$

where  $C_0$  comes from (4.5).

Figure 10 shows this spray generation function for a range of wind speeds. Finding  $U_{N10}$  and  $U_{A/3}$  values to use in (5.1) is crucial. To compute these, I first run the new bulk flux algorithm that Andreas et al. (2015) describe; from sea surface temperature ( $T_s$ ) and from wind speed ( $U_r$ ), air temperature ( $T_a$ ), and relative humidity ( $RH_r$ ) at arbitrary reference height  $r$ , it



computes, among other quantities, the friction velocity  $u_*$  and the Obukhov length  $L$ . Equations like (3.1) and (3.2) yield  $U_{A_{1/3}}$  and  $U_{N10}$  as

$$U_{A_{1/3}} = U_r + \frac{u_*}{k} \left[ \ln \left( \frac{A_{1/3}}{r} \right) - \psi_m \left( \frac{A_{1/3}}{L} \right) + \psi_m \left( \frac{r}{L} \right) \right] \quad (5.2)$$

and

$$U_{N10} = U_r + \frac{u_*}{k} \ln \left( \frac{10}{r} \right). \quad (5.3)$$

For comparison with an open ocean spray generation function, I also plot in Fig. 10 the function that Andreas et al. (2010) created by smoothly joining the bubbles-only function from Monahan et al. (1986) with the large-radius function that Fairall et al. (1994) formulated from an earlier function from Andreas (1992). After reviewing the field, Andreas (2002b) had concluded that the Monahan et al. function provides an “anchor” for predicting the generation of small droplets over the open ocean while the Fairall et al. function has the best overall properties for high winds and larger droplets.

Furthermore, the merging is fairly easy: Both functions take as their wind speed dependence the whitecap coverage ( $W$ ) that Monahan and O’Muircheartaigh (1980) deduced,

$$W(U_{10}) = 3.8 \times 10^{-6} U_{10}^{3.4}. \quad (5.4)$$

In this,  $W$  is the fractional whitecap coverage, and  $U_{10}$  is the wind speed at 10 m.

In Fig. 10, (5.1) is roughly three orders of magnitude larger than the joint Monahan and Fairall function for droplets smaller than about 30  $\mu\text{m}$  in radius. As the radius increases, this difference decreases until the level of (5.1) extrapolated to  $r_0 = 200 \mu\text{m}$  is very close to the level of the joint Monahan and Fairall function. The large-radius slope of my new function is also very close to the large-radius slope of the Monahan and Fairall function.

346 Previously, de Leeuw et al. (2000) measured surf zone production at the Scripps pier in  
347 La Jolla, California. Likewise, van Eijk et al. (2011) measured surf zone production at La Jolla  
348 and also at the Field Research Facility in Duck, North Carolina. Both of these surf zones are  
349 characterized by gently sloping beaches in contrast to the abrupt, rocky shoreline and the absence  
350 of a beach at Mt. Desert Rock. de Leeuw et al. concluded that the breaking waves at the La Jolla  
351 site enhanced spray production by up to two orders of magnitude. For their two sites, van Eijk et  
352 al. concluded that the surface zone added 0.7 to one order of magnitude to the spray  
353 concentration. Remember, though, both groups observed spray droplets with radii no bigger than  
354 30  $\mu\text{m}$ .

355 The next section continues this discussion of the enhanced spray production that I  
356 observed.

357

## 6. Discussion

### *a. Footprint analysis*

The explanation for the magnitude of the spray flux observed at Mt. Desert Rock is intimately tied to the upwind footprint that influenced measurements at the cloud imaging probe. Classically, the flux footprint is a function of distance ( $x$ ) upwind from an instrument, which is at height  $z_m$ ; the origin of this distance is at the instrument. By integrating over all  $x$  the surface flux at location  $x$  multiplied by the footprint function at  $x$ , we derive the flux at the origin and at height  $z_m$  that the instrument sees (e.g., Horst and Weil 1992, 1994; Wilson 2015).

Besides  $z_m$ , which is 3.24 m for the cloud imaging probe, another parameter that is important in most footprint analyses is the aerodynamic roughness length  $z_0$ . For a typical wind speed in my dataset,  $12 \text{ m s}^{-1}$ , I estimate  $z_0 = 3.4 \times 10^{-4} \text{ m}$ . Hence,  $z_m/z_0$ , another important quantity, is about 9500. The height of the atmospheric boundary layer,  $h$ , and the ratio  $z_m/h$  are also required in some footprint analyses. Without measurements of  $h$ , I surmise that it was rarely less than 400 m; therefore,  $z_m/h \leq 0.008$ .

The footprint function is zero for some distance immediately upwind of the instrument (Horst and Weil 1994; Hsieh et al. 2000; Wilson 2015). In essence, material escaping the surface too close to the instrument does not have time to reach height  $z_m$  and be observed before it is blown beyond the instrument. I denote this distance  $X$  for “excluded.”

The total upwind extent of the flux footprint itself I denote as  $F$  (in meters). From figures in Kljun et al. (2004; e.g., Fig. 1), I estimate that, for the given values of  $z_m$ ,  $z_0$ ,  $h$ , and stratification, the footprint is approximately zero for  $F$  larger than about 200 m. In other words, the CIP is most sensitive to the surface within 200 m upwind from it. Meanwhile, the peak of the footprint function—the region of upwind fetch that contributes the most to observations at

height  $z_m$ —is roughly 50–70 m upwind of the instrument (Horst and Weil 1994, Fig. 3; Kljun et al., Fig. 1). From Fig. 1, we can therefore conclude that most of the spray reaching the cloud imaging probe originated in or near the surf zone.

Let us suppose that this surf zone has a width  $S$ . But  $S$  is not constant; I observed it to increase with wind speed (and the resulting wave energy) such that it was about 30 m wide for the highest wind speeds we encountered on Mt. Desert Rock, about  $20 \text{ m s}^{-1}$ . As a crude estimate to model this wind speed effect on the surf zone, I use

$$S = 30 \left( \frac{U_{N10}}{20} \right)^3, \quad (6.1)$$

where  $S$  is in meters when  $U_{N10}$  is in  $\text{m s}^{-1}$ . This choice of a cubic dependence on  $U_{N10}$  recognizes that the energy flux that the wind puts into the ocean—and which, in turn, builds the waves that create the surf zone—scales with the cube of the wind speed (e.g., Wu 1979).

With this conceptual framework, I can predict how the quantity of spray produced in a surf zone might differ from spray over the open ocean. Over the open ocean, the spray measured by a cloud imaging probe at height  $z_m$  would scale something like

$$\text{Ocean: } W(U_{10})(F - X). \quad (6.2)$$

The spray actually measured by the CIP at Mt. Desert Rock, on the other hand, would scale like

$$\text{MDR: } W(U_{10})(F - S - R) + 1 \cdot \gamma \cdot S + 0 \cdot R. \quad (6.3)$$

Both of these equations rest on the common practice of inferring spray production from whitecap coverage.

In (6.2) and (6.3),  $W(U_{10})$  is the fractional whitecap coverage for the open ocean as estimated from (5.4). In (6.3),  $R$  is the distance over rock from the CIP to the shoreline on Mt. Desert Rock; I estimate it as, typically, 30 m (see Fig. 1). This portion of the footprint obviously

produces no spray; the footprint function is thus zero here. In contrast, the surface zone is one continuously renewed whitecap; the fractional whitecap coverage is 1 here (de Leeuw et al. 2000; i.e., the 1 multiplying the  $S$  term in (6.3)). Moreover, as I will discuss shortly, the surf zone is more productive white water than would be characterized by just whitecap coverage, (5.4). Therefore, I include the  $\gamma$  coefficient in the  $S$  term and expect  $\gamma$  to be one or greater.

By taking the ratio of (6.3) to (6.2), we can estimate how productive the surf zone at Mt. Desert Rock is compared to the open ocean:

$$Ratio = \frac{W(U_{10})(F - S - R) + \gamma S}{W(U_{10})(F - X)}. \quad (6.4)$$

For demonstration purposes and because  $R$  and  $X$  are relatively small compared to  $F$ , I set  $X = R$ . Then (6.4) reduces to

$$Ratio = \frac{\gamma S}{W(U_{10})(F - R)} + 1 - \frac{S}{F - R}. \quad (6.5)$$

The white water in the surf zone more closely resembles a stage A whitecap than a stage B whitecap. Stage A whitecaps are associated with actively breaking waves, while stage B whitecaps result from the rising, decaying bubble plumes left after a wave breaks (Monahan and Lu 1990). The surf zone at Mt. Desert Rock during winds of  $10 \text{ m s}^{-1}$  and higher was a very energetic and turbulent region of total white water and continually breaking waves (cf. Brocchini and Peregrine 2002).

Woolf et al. (1987) and Cipriano et al. (1987) studied spray formation in a laboratory whitecap simulation tank. Although they could measure only spray droplets with radii of about  $10 \text{ }\mu\text{m}$  or less, their result are, nevertheless, suggestive of what we might see on Mt. Desert Rock. Figures 4 and 5 in Woolf et al. and Fig. 2 in Cipriano et al. suggest that a newly formed whitecap (the stage A whitecap) produces about an order of magnitude more spray droplets per

unit time than the later decaying phase (stage B) of the whitecap. On reevaluating these papers, Ed Monahan (2015, personal communication) estimated that the production of these droplets, which have radii at the small end of my spectrum, may even be up to two orders of magnitude higher in stage A whitecaps than in stage B whitecaps.

These studies by Woolf et al. (1987) and Cipriano et al. (1987) generally quantified only the spray production by bursting bubbles—that is, film and jet droplets. In the surf zone, with an onshore wind, other mechanisms can also create spray droplets (e.g., Peregrine 1983; Monahan et al. 1986; Andreas et al. 1995, Fig. 1; Brocchini and Peregrine 2002). Spume droplets, which the wind tears right off the wave crests (e.g., Soloviev et al. 2012), are generally larger than film and jet droplets. In the very turbulent surf zone, where waves reflected from the steep shore collide with incoming waves from the ocean, so-called splash and chop droplets also occur. It is therefore not implausible to speculate that these latter processes, especially, can enhance the spray production another order of magnitude.

In summary, spray production in a surf zone at a rocky shoreline, where white water is ubiquitous and continually renewed, could be 10 to 1000 times higher at comparable winds speeds than over the open ocean, where spray production predominantly comes from stage A and stage B whitecaps. Therefore, Fig. 11 displays the ratio in (6.5) for  $\gamma$  ranging from 1 to 1000.

Although their geometry was somewhat different than for my observations on Mt. Desert Rock, the  $\gamma = 1$  and  $\gamma = 10$  cases in Fig. 11 approximate the data that de Leeuw et al. (2000) and van Eijk et al. (2011) obtained downwind of far less energetic surf zones over sloping beaches. Even if the breakers on their beaches were not more effective spray producers than open ocean whitecaps—that is, assuming  $\gamma = 1$ —Fig. 11 suggests that the spray production would still be enhanced by a factor of 3 or 4 because of the increased whitecap coverage.

Meanwhile, according to Fig. 11, a  $\gamma$  value between 100 and 1000—which according to my literature review seems to be possible—would explain the observed spray concentrations and spray generation function (Fig. 10), where the Mt. Desert Rock values are about three orders of magnitude larger than over the open ocean.

#### *b. Parameterizing the spray*

The debate on how to parameterize near-surface spray concentration and the spray generation function has gone back and forth for about 35 years. One approach assumes that the shape of the spray distribution with radius at formation  $r_0$  is independent of forcing variables like wind speed, wave field, or water temperature. Then the near-surface spray concentration (as a function of just radius and wind speed for demonstration purposes) could be formulated as the product of a shape function,  $f(r_0)$ , and a forcing function,  $g(U_{10})$ :

$$C_0(r_0, U_{10}) = f(r_0)g(U_{10}). \quad (6.6)$$

de Leeuw et al. (2011) reviewed this concept; and it has found application in spray generation functions formulated by Monahan et al. (1986, their bubbles-only function), Fairall et al. (1994), and Andreas et al. (2010), among others.

The second school of thought supposes that the shape of the droplet spectrum depends on the forcing variables; and, therefore, separating the size function and the forcing function as in (6.6) is not possible. Monahan et al. (1983) seemed to document this change in the droplet spectrum with wind speed when they observed enhanced droplet counts for large droplets at higher wind speeds. Miller and Fairall (1988) put this approach in practice when they synthesized from four datasets a spray generation function for which the shape changed with wind speed. Andreas (1992), for example, was an early user of this Miller and Fairall function.

Smith et al. (1993) and later Smith and Harrison (1998) likewise derived spray generation functions for which the shape of the droplet spectrum changed with wind speed.

My observations, however, come down on the side of (6.6)—that the droplet spectrum does not change shape significantly with wind speed or other forcing variables for wind speeds between 5 and 17 m s<sup>-1</sup>. In view of Figs. 5, 6, and 7, this conclusion is very robust.

Admittedly, the references cited in this section were all to open ocean conditions. Hence, it is not clear that the data from Mt. Desert Rock can be extended to the open ocean and, thereby, can add weight to either side of the argument on how to parameterize  $C_0$  and  $dF/dr_0$ . I, nevertheless, felt it essential to interpret my data in the context of this debate.

### *c. Height profile of the spray*

To assess icing and sea salt accumulation on structures downwind of a shoreline where spray is forming, we need to model the profile of the spray as a function of vertical coordinate  $z$ . Equations that have appeared earlier provide the solution. Namely, we can rearrange (3.5) to get the spray concentration profile:

$$C(z, r_0, U_{N10}) = C_0(r_0, U_{N10}) \left( \frac{z}{A_{1/3}} \right)^{-V_g(r_0)/k u_* f_s}. \quad (6.7)$$

Furthermore, we can substitute (4.5) for  $C_0(r_0, U_{N10})$ . Equation (3.6) shows how to calculate  $f_s$ .

To continue with the calculation, readers can use their favorite algorithms for computing  $V_g$  and  $u_*$ . Alternatively, they can retrieve from

<http://people.nwra.com/resumes/andreas/software.php> a bulk flux algorithm that Andreas et al. (2015) developed for computing  $u_*$  over the ocean, among other fluxes, and a second algorithm for fast microphysical calculations that include computing  $V_g$  (Andreas 2005).



## 7. Conclusions

With increasing wind speed, the surf zone at the rocky shore of Mt. Desert Rock became increasingly energetic. Active wave breaking, ubiquitous stage A whitecaps, and continuous turbulent white water grew oceanward from the shoreline with increasing winds. A cloud imaging probe placed a few tens of meters downwind from this surf zone counted the spray droplets generated there.

For 10-m, neutral-stability wind speeds ( $U_{N10}$ ) between 5 and 17 m s<sup>-1</sup>, I thus documented the near-surface concentration of spray droplets in 12 12.5- $\mu$ m-wide bins with centers from 6.25 to 143.75  $\mu$ m. One of the main results is that the shape of these near-surface concentration spectra,  $C_0(r_0, U_{N10})$ , as a function of droplet radius at formation,  $r_0$ , is independent of wind speed. I could, thus, formulate an expression for the near-surface concentration in terms of two independent functions:

$$C_0(r_0, U_{10}) = f(r_0)g(U_{10}), \quad (7.1)$$

where  $f(r_0)$  is a shape function and  $g(U_{N10})$  is a wind speed function. Equations (4.3) and (4.4), respectively, give these two functions.

Because of the high energy in the surf zone and the fact that a footprint analysis suggests that the cloud imaging probe focused preferentially on spray coming from the surf zone, the measured spray concentrations are two to three orders of magnitude higher than those measured over the open ocean. Waves crashing against rocks also produce one to two orders of magnitude more spray than waves breaking on sloping beaches.

The spray generation function derived from these near-surface concentration measurements reiterates how much more productive the surf zone is than is the open ocean. Figure 10 shows that, at least for droplets smaller than about 30  $\mu$ m in  $r_0$ , the surf zone at Mt.

Desert Rock was three orders of magnitude more productive than the open ocean.

For droplets above 100  $\mu\text{m}$  in radius, on the other hand, the Mt. Desert Rock spray generation function is comparable to the open ocean function. There are two possible explanations for this convergence for large radii. Either the joint Monahan et al. (1986) and Fairall et al. (1994) function overestimates the generation rate of the largest droplets or, at the CIP site on Mt. Desert Rock, many of the larger droplets settled out of the air flow before the CIP could count them. Both explanations are plausible because the counting statistics for the CIP were best for the smaller droplets, while the joint Monahan and Fairall function for open ocean spray generation shown in Fig. 10 is also most reliable for the smaller droplets. In summary, the orders-of-magnitude difference in spray concentration and in spray generation (Fig. 10) between Mt. Desert Rock and the open ocean is robust for droplet radii less than 50–100  $\mu\text{m}$ .

Because these observations on Mt. Desert Rock are the first spray measurements at a rocky shoreline, I cannot say how general the results are. The footprint analysis in Section 6a provides justification for presuming that production in the surf zone at a rocky shoreline should be 2–3 orders of magnitude higher than over the open ocean. Moreover, its correct order-of-magnitude prediction for spray production over a sloping, sandy beach provides validation for that analysis. Consequently, although (4.5) and (5.1) may not be perfectly transferrable to other abrupt shores, they should be useful planning tools for evaluating how hazardous spray icing and sea salt might be for artificial islands currently built or planned for the high-latitude ocean.

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## APPENDIX

### Obtaining Droplet Concentration from the Cloud Imaging Probe

The cloud imaging probe (CIP; from Droplet Measurement Technologies, Inc., Boulder, Colorado) uses single-particle optical imaging with a linear array of 64 photodetectors to count and size droplets. The following equations that I used to process the raw CIP data come from the user's manuals (Anonymous 2009, 2012) and from software that Chris Fairall (2012, personal communication) shared with me.

The CIP uses a red laser; the wavelength is  $\lambda = 0.660 \mu\text{m}$ . The resolution in size bins is  $R = 25 \mu\text{m}$ : that is, the CIP counts droplets in size bins that increase from zero in steps of  $25 \mu\text{m}$  in diameter. The CIP has a linear array of 64 (= ND) diode detectors; it thus can sort droplets into 62 (= NB) bins, each  $25\text{-}\mu\text{m}$  wide.

I do the analysis, however, in terms of droplet radius; thus, the radius resolution is  $\Delta r = R/2 = 12.5 \mu\text{m}$ . With 62 CIP bins of width  $\Delta r$ , the upper radius limit for each bin ( $Bin_{Hi}$ ) increases as  $12.5i$ , where  $i = 1, 62$ . Hence,  $Bin_{Hi} = 12.5, 25, 37.5, 50, \dots, 762.5, 775 \mu\text{m}$ . Likewise, the lower limit on each radius bin ( $Bin_{Lo}$ ) goes as  $12.5(i - 1)$ , where  $i = 1, 62$ . That is,  $Bin_{Lo} = 0, 12.5, 25, 37.5, \dots, 750, 762.5 \mu\text{m}$ . My convention is to use the center radius of each bin to denote droplets counted by the CIP at a given radius. The center radius of a bin (in  $\mu\text{m}$ ) is  $Bin_{cent} = 6.25 + 12.5(i - 1)$ , where  $i = 1, 62$ .

On Mt. Desert Rock, the counting statistics for 30 minutes of sampling were poor for droplets beyond the bin centered at  $143.75 \mu\text{m}$ . Hence, my plots show only droplets centered in the 12 bins  $6.25, 18.75, 31.25, 43.75, \dots, 131.25, 143.75 \mu\text{m}$ .

Approximately every second, the CIP reported the number of droplets counted in each of its 62 bins. Call this one-second value the count  $K$  in bin  $i$  at time  $j$ ,  $K(j, i)$ . The number of

570 droplets counted in bin  $i$  in 30 minutes is simply the sum of all these counts:

$$571 \quad \overline{K}(i) = \sum_{j=1}^{\sim 1800} K(j, i). \quad (A1)$$

572 To find the droplet concentration in bin  $i$  for the 30 minutes, we must divide the bin sum  
573 by the total volume of air sampled ( $V$ ) and by the bin width,  $\Delta r$ :

$$574 \quad C(i) = \frac{\overline{K}}{V \Delta r}. \quad (A2)$$

575 This has units of a droplet concentration: number of droplets per cubic meter of air per  
576 micrometer increment in droplet radius.

577 The volume  $V$  depends on the size bin. We first calculate the length of the diode array  
578 for droplets of size  $i$ :

$$579 \quad L_{CIP}(i) = 2 \cdot 0.001 \cdot \Delta r (ND - i - 1), \quad (A3)$$

580 where  $i = 1, 62$  and the 0.001 converts  $\Delta r$  in micrometers to millimeters. Thus, the lengths of the  
581 bins are  $L_{CIP}(1) = 1.550$  mm,  $L_{CIP}(2) = 1.525$  mm,  $L_{CIP}(3) = 1.500$  mm, ...,  $L_{CIP}(61) = 0.050$  mm,  
582  $L_{CIP}(62) = 0.025$  mm.

583 The second length scale is the distance across the laser array,  $zz(i)$ . Again, this distance is  
584 a function of size bin but also of the laser optics. From Chris Fairall (2012, personal  
585 communication),

$$586 \quad zz(i) = \min \left\{ 1580 \text{DOF0} \left[ 0.001 \text{Bin}_{Hi}(i) \right]^2, 100 \text{ mm} \right\}, \quad (A4)$$

587 where  $zz$  is also in millimeters and  $\text{Bin}_{Hi}(i)$  is the upper radius limit of the  $i$ th bin.

588  $\text{DOF0} = 2.4054$  is related to the depth of field of the laser array. Equation (A4) gives

589  $zz(1) = 0.594$  mm,  $zz(2) = 2.375$  mm,  $zz(3) = 5.344$  mm, ...,  $zz(12) = 85.51$  mm,

590  $zz(13) = 100$  mm. And for all higher bins,  $zz$  is also 100 mm.

591 The final dimension for calculating the volume  $V$  in (A2) is related to the flow of air  
 592 through the laser array. This is just  $\overline{U}_\perp \Delta t$ , where  $\overline{U}_\perp$  is the average wind speed perpendicular  
 593 to the laser array during the 30-minute sampling (or sometimes shorter) period ( $\Delta t$ ) as measured  
 594 by the Gill sonic anemometer attached to the cloud imaging probe. I made no corrections for the  
 595 sonic's being 48 cm above the laser array.

596 Putting this last result together with (A3) and (A4) in (A2), I finish the algorithm for  
 597 computing the spray droplet concentration in bin  $i$ :

$$598 \quad C(i) = \frac{10^6 \overline{K}_i}{L_{CIP}(i) \overline{z z}(i) \overline{U}_\perp \Delta t \Delta r} . \quad (A5)$$

599 Because  $L_{CIP}$  and  $\overline{z z}$  are both expressed in millimeters, we must multiply the right side of (A5) by  
 600  $10^6$  to obtain  $C(i)$  in  $\text{m}^{-3} \mu\text{m}^{-1}$ .

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## CAPTIONS OF FIGURES

730 FIG. 1. Mt. Desert Rock. The light gray shading is the island at high tide; the dark gray, the  
731 island at low tide. The range between high and low tide is about 3 m. Orange objects are  
732 permanent structures: The oval is the lighthouse; the big square is the lightkeeper's house. The  
733 red circle on the small square is the cloud imaging probe and associated sonic  
734 anemometer/thermometer mounted on the foghorn platform. The three-legged symbol denotes  
735 the "turbulence tripod." The quadrant 260° to 7° indicates the only wind directions I retained for  
736 my analyses. The arcs at 50 and 75 m show that all samples collected by the cloud imaging  
737 probe were within 75 m of the water; and, at high tide, most were much closer.

738 FIG. 2. The cloud imaging probe from Droplet Measurement Technologies and the Gill sonic  
739 anemometer/thermometer mounted on the foghorn platform on Mt. Desert Rock.

740 FIG. 3. Wind speed, air temperature, and relative humidity during the experiment on Mt. Desert  
741 Rock (MDR). All legends refer to all panels. "MDR NOAA" identifies the NOAA instruments  
742 on the lighthouse; likewise, "Matinicus" denotes the NOAA instruments on Matinicus Rock.  
743 "Gill Sonic on MDR" is wind speed from the Gill sonic anemometer associated with the cloud  
744 imaging probe. "Our Data" identifies the wind speed and temperature data from the turbulence  
745 tripod.

746 FIG. 4. Surface water temperature and salinity and significant wave height ( $H_{1/3}$ ) during the  
747 experiment on Mt. Desert Rock. In the temperature and salinity panels, the data identified as  
748 "Ours" are from manual bucket samples. In the wave height panel, our estimate of  $H_{1/3}$  comes  
749 from the Andreas and Wang (2007) algorithm and the wind speed from the Gill sonic  
750 anemometer.

751 FIG. 5. Near-surface spray droplet concentration spectra (i.e.,  $C_0$  from (3.5)) for wind speeds  
 752 ( $U_{N10}$ ) between 6 and 10 m s<sup>-1</sup>. The black and red curves distinguish between measurements  
 753 made during high water and low water, respectively. The green curve is the fit to these  
 754 concentration spectra, (4.5), where the  $U_{N10}$  used to calculate each green curve is the middle  
 755 value of the indicated wind speed range.

756 FIG. 6. As in Fig. 5 but for wind speeds between 10 and 17 m s<sup>-1</sup>.

757 FIG. 7. All the concentration spectra (e.g., Figs. 5 and 6) measured in wind speeds ( $U_{N10}$ ) of  
 758 5 m s<sup>-1</sup> and higher are nondimensionalized with the respective concentration measured in the  
 759 radius bin centered at 6.25  $\mu$ m. Hence, all spectra are identically one for  $r_0 = 6.25 \mu$ m. The plot  
 760 still distinguishes measurements made during high water from those made during low water.  
 761 The plot also shows the bin medians for all the data and, individually, for the high-water and  
 762 low-water data. The small-radius bins and the large-radius bins fall along straight lines in this  
 763 log-log plot (the two black lines). I thus represent the median nondimensional spectrum with a  
 764 hyperbola, (4.3) with  $a = 0.10$ .

765 FIG. 8. All concentration data in the 333 runs are normalized and plotted against  $U_{N10}$ . The  
 766 normalization is for each radius bin such that all concentrations measured in that bin are divided  
 767 by the bin average. The data are identified as to whether they were collected during high water  
 768 or low water. Three fitting lines are shown: one calculated using least-squares linear regression  
 769 as y-versus- $x$ , one taken as the bisector of y-versus- $x$  and  $x$ -versus- $y$  fits, and one for which a  
 770  $U_{N10}^3$  dependence is assumed.

771 FIG. 9. The near-surface spray concentration data (i.e.,  $C_0$ ) for the bin centered at  $r_0 = 6.25 \mu\text{m}$   
772 are plotted versus the neutral-stability wind speed at 10 m,  $U_{N10}$ . The blue line is the best-fitting  
773 cubic relation through these data, (4.4).

774 FIG. 10. The Mt. Desert Rock (MDR) spray generation function, (5.1), as a number flux for  
775 various values of the wind speed at a reference height of 10 m,  $U_{10}$ . For these calculations, the  
776 surface temperature ( $T_s$ ) was  $1^\circ\text{C}$ ; the air temperature ( $T_r$ ),  $0^\circ\text{C}$ ; the relative humidity ( $RH_r$ ),  
777 80%; the surface salinity, 34 psu; and the barometric pressure, 1000 mb. For comparison, the  
778 plot also shows the joint Monahan et al. (1986) and Fairall et al. (1994) function (from Andreas  
779 et al. 2010).

780 FIG. 11. The ratio of surf-zone production to open-ocean production of spray, as predicted by  
781 (6.5), is plotted as a function of 10-m wind speed ( $U_{10}$ ) for the  $\gamma$  values indicated. As explained  
782 in the text, in (6.5)  $F = 200 \text{ m}$ ,  $R = 30 \text{ m}$ ,  $S$  comes from (6.1), and  $W(U_{10})$  comes from (5.4).

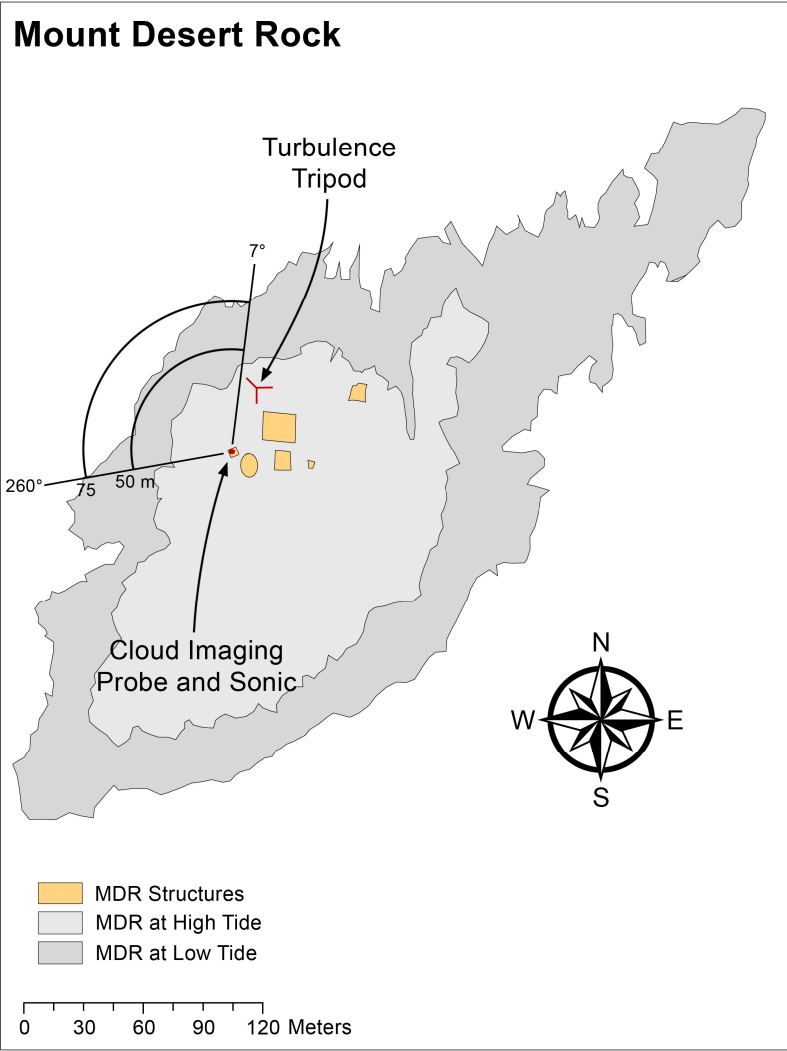


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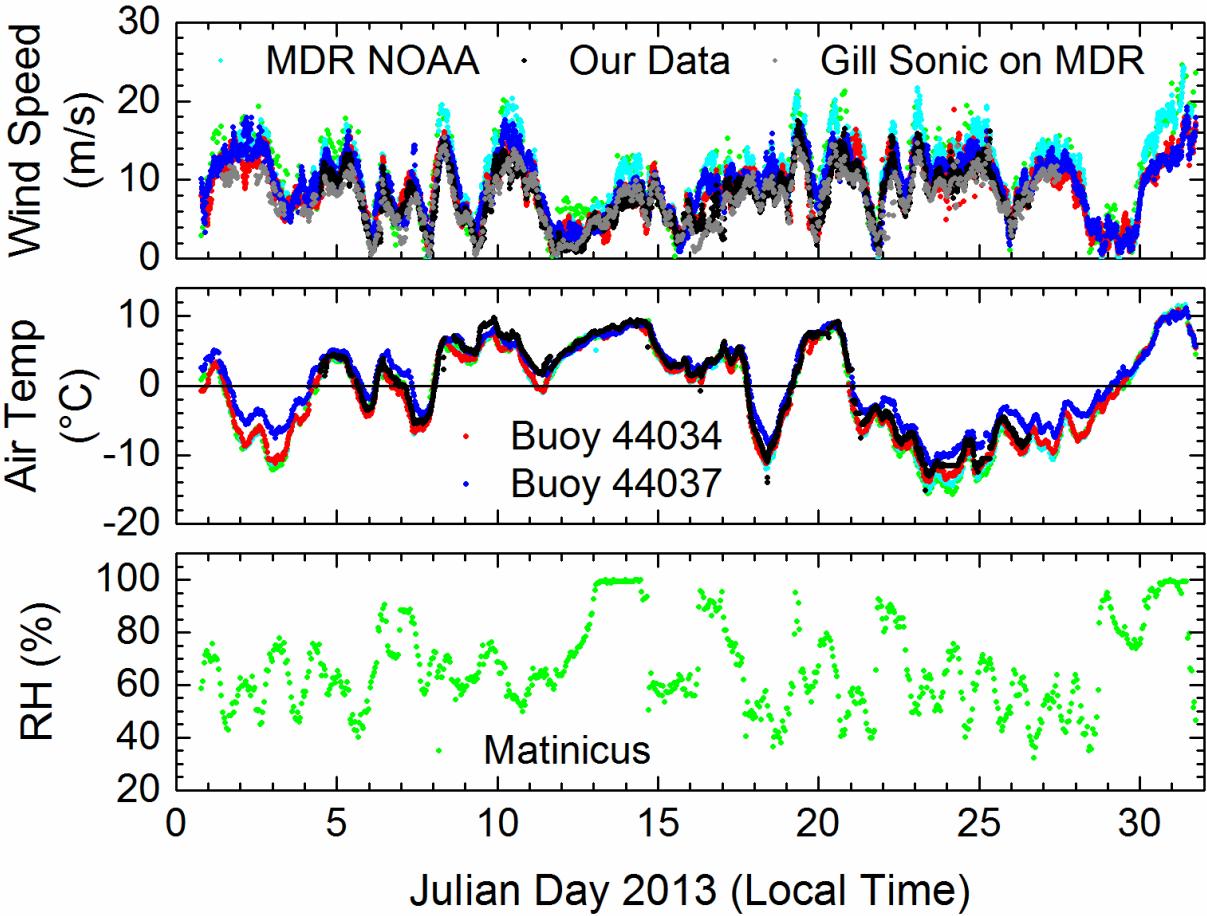


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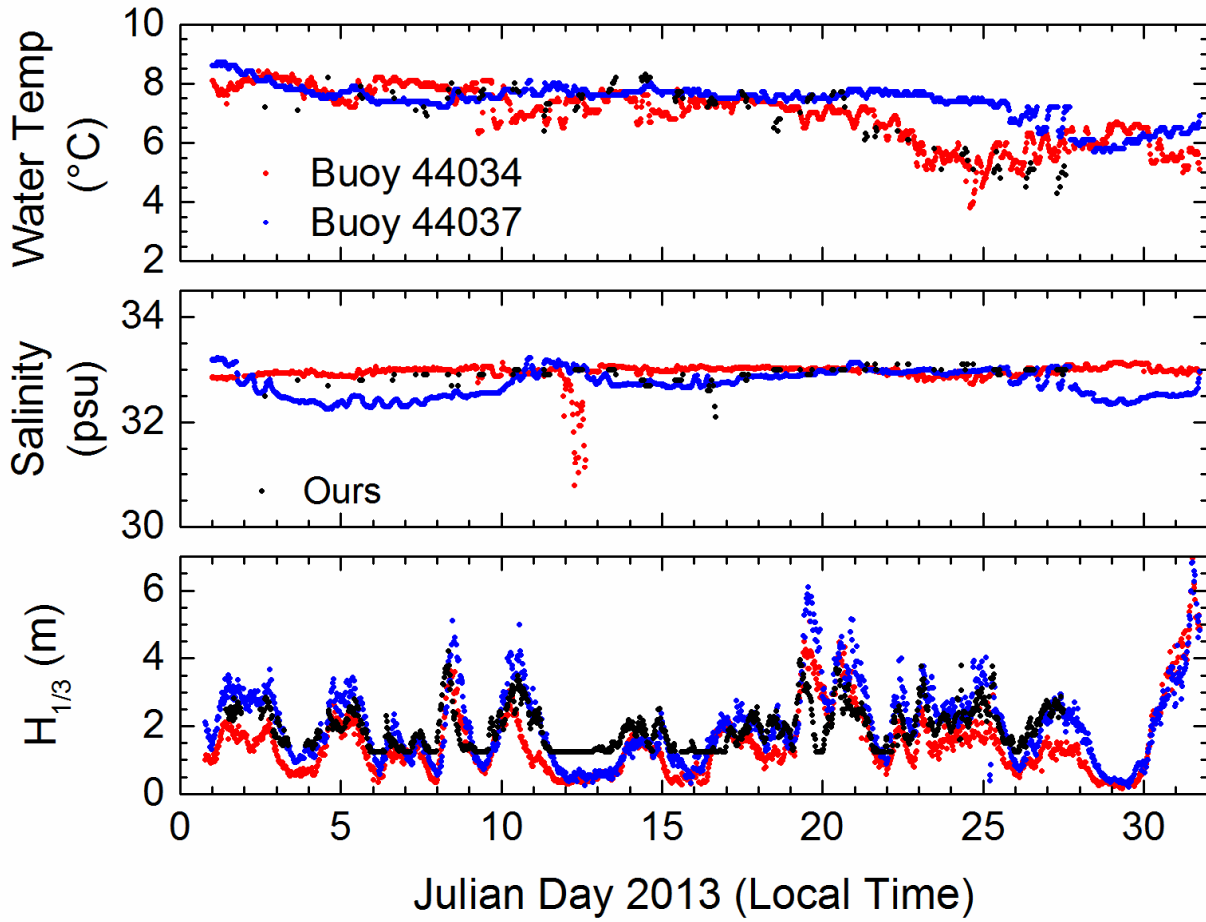


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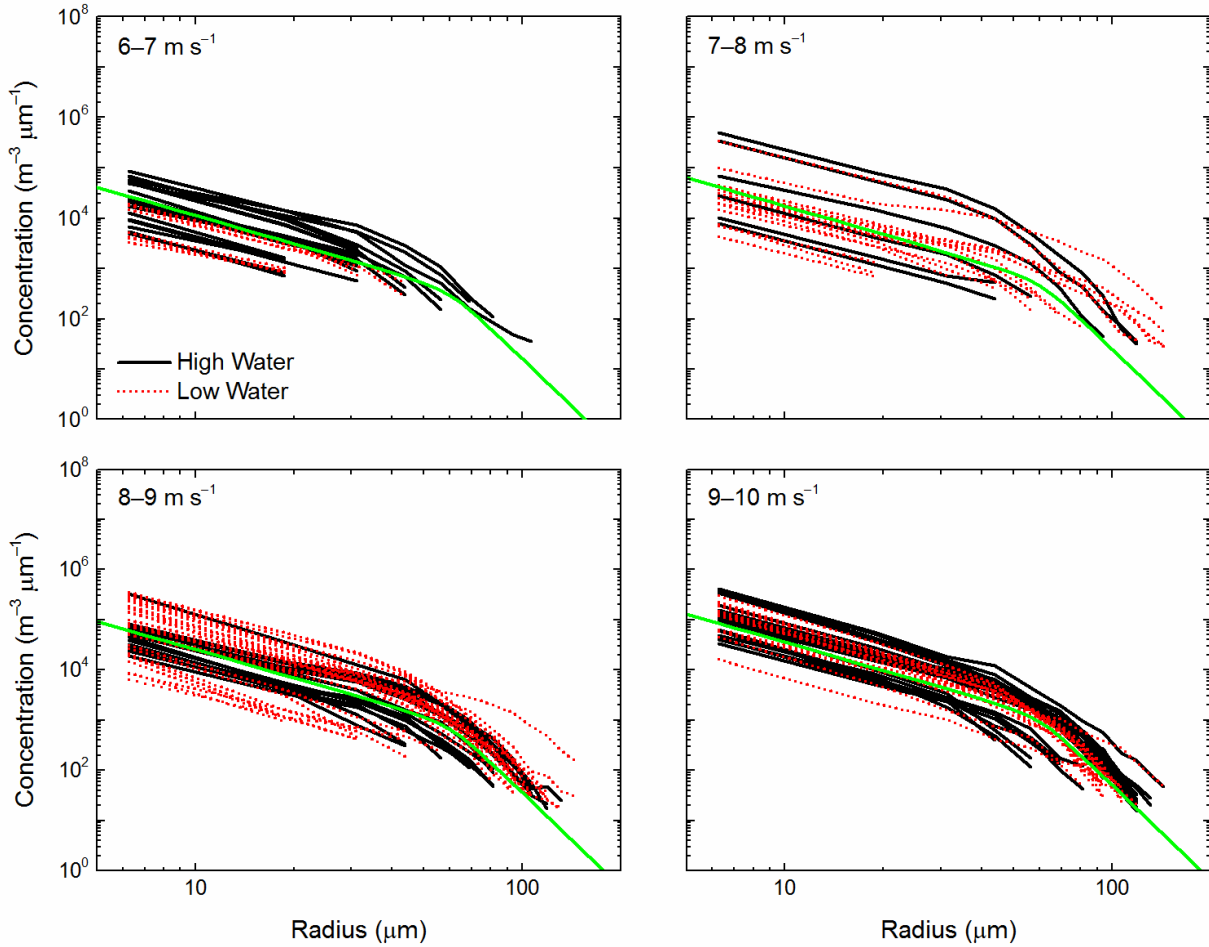


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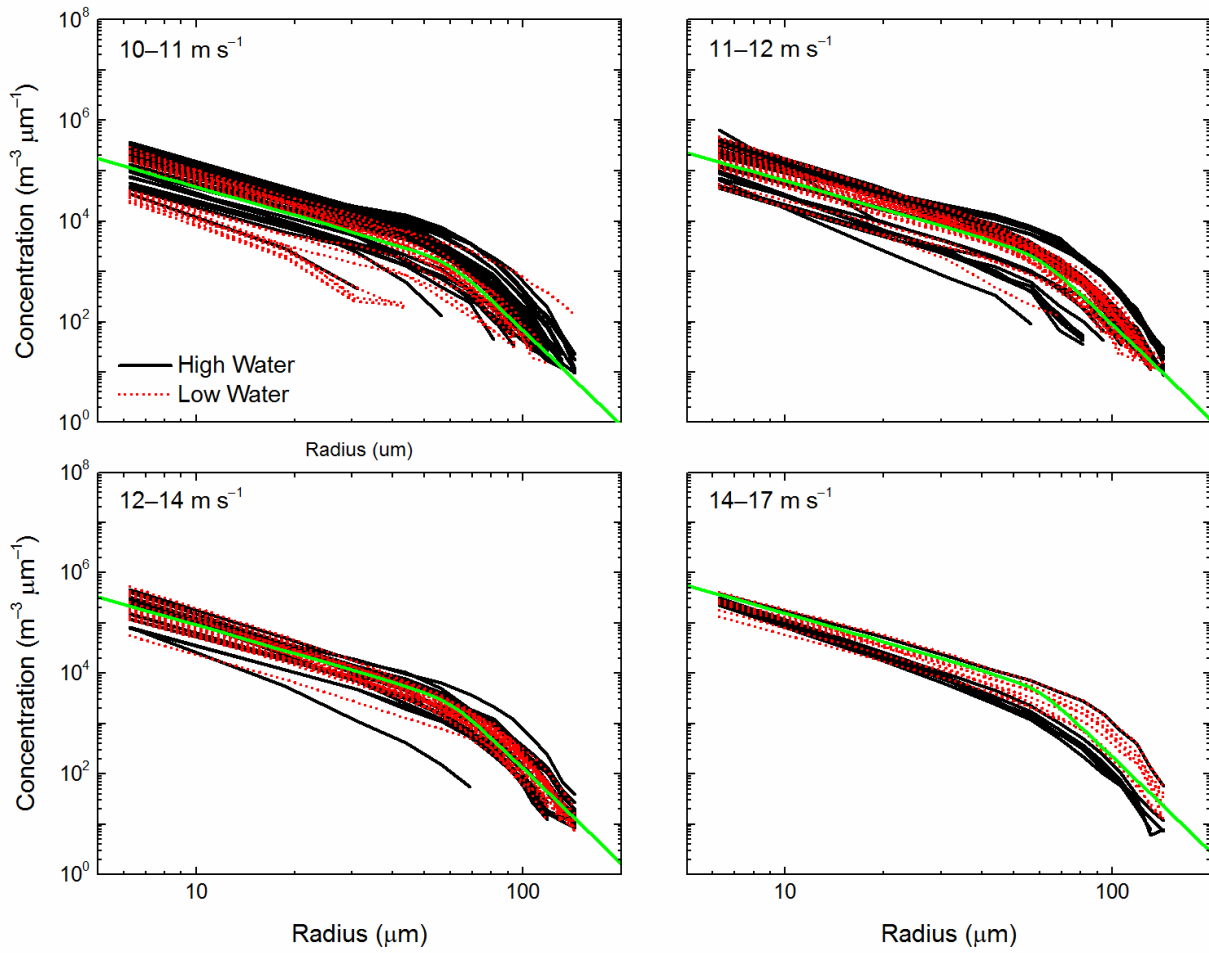


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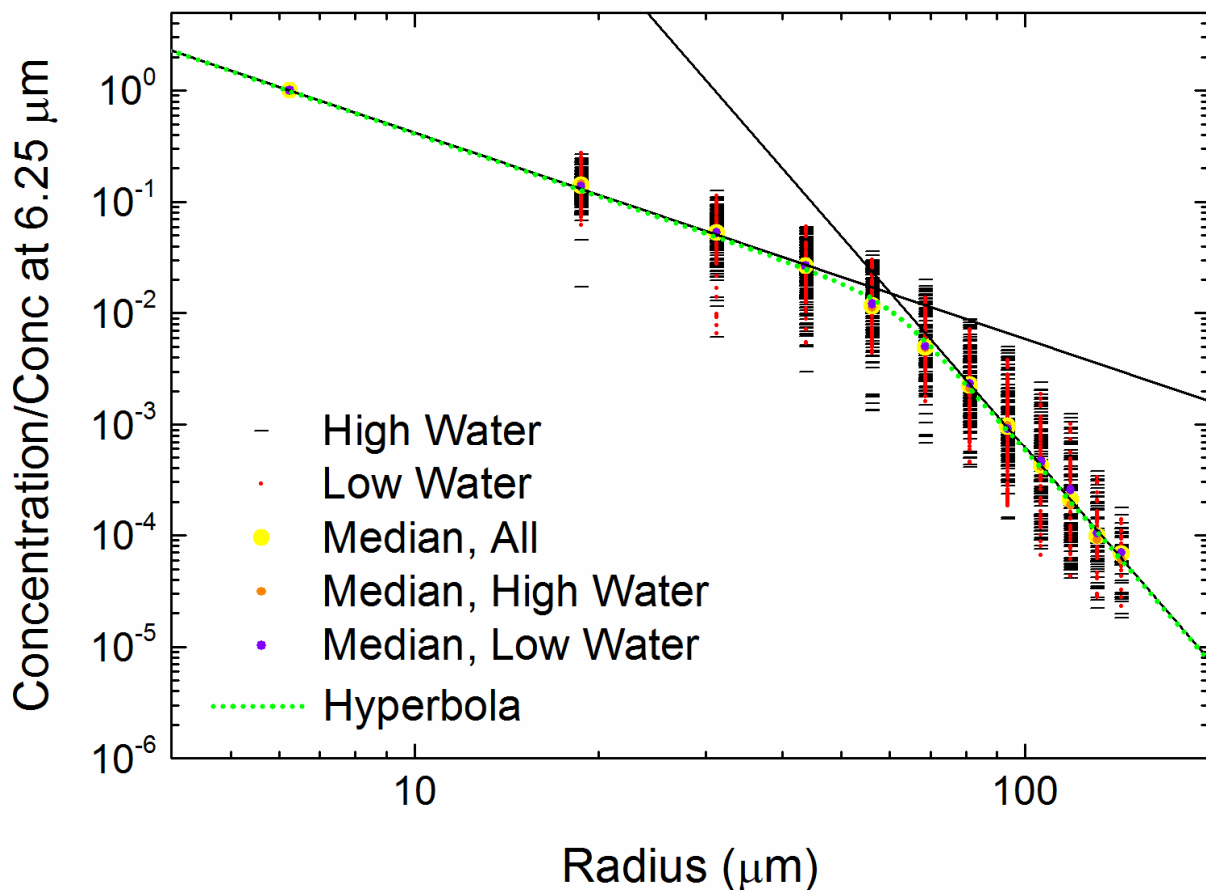


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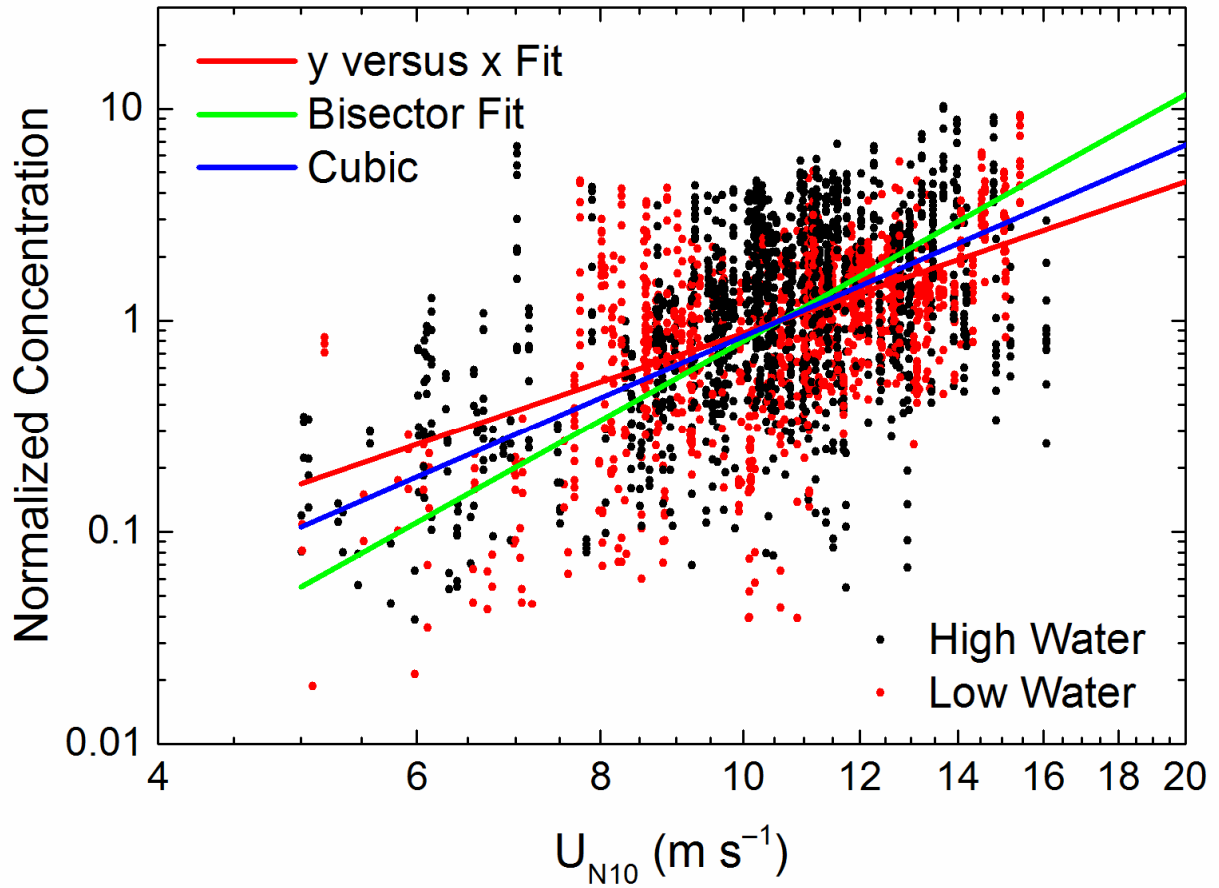


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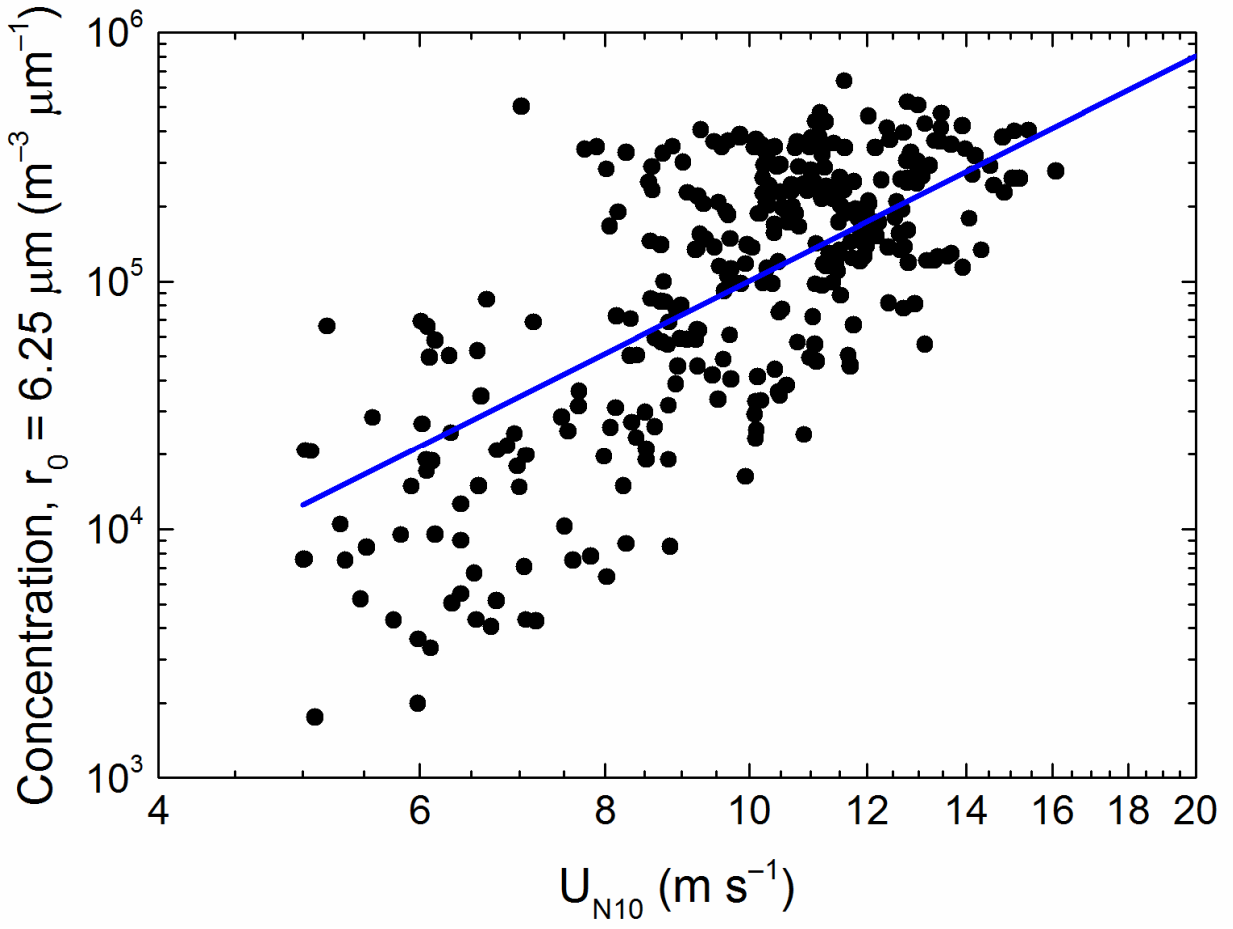


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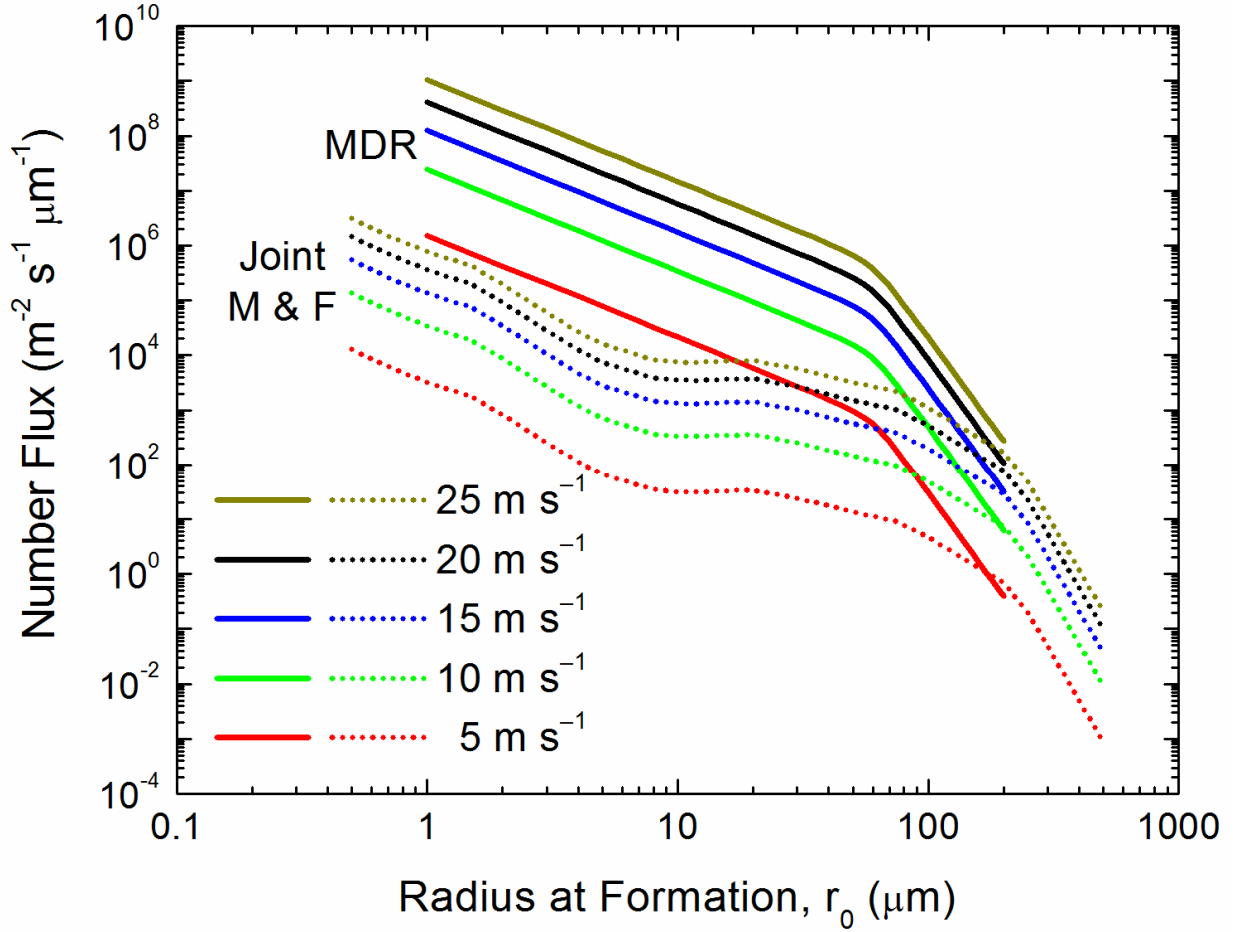


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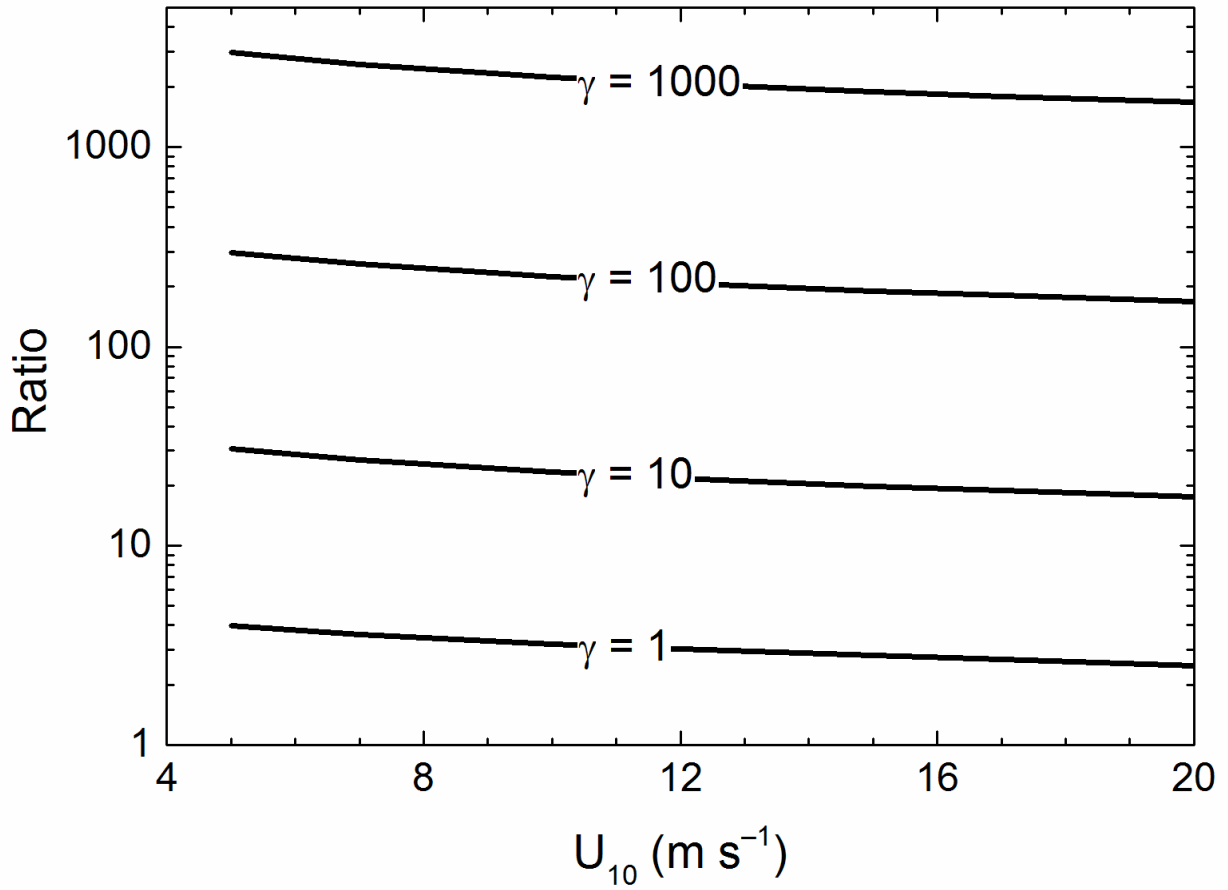


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